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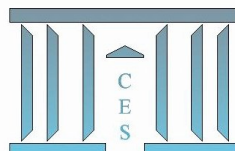
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**Three different ways synchronization can cause
contagion in financial markets**

Naji MASSAD, Jørgen-Vitting ANDERSEN

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Three different ways synchronization can cause contagion in financial markets.

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Abstract: We introduce tools from statistical physics, to capture the dynamics of three different pathways, in which the synchronization of human decision making could lead to turbulent periods and contagion phenomena in financial markets. The first pathway is caused when stock market indices, seen as a set of coupled integrate-and-fire oscillators, synchronize in frequency. The integrate-and-fire dynamics happens due to "change blindness", a trait in human decision making where people have the tendency to ignore small changes, but take action when a large change happens. The second pathway happens due to feedback mechanisms between market performance, and the use certain (decoupled) trading strategies. The third pathway can take place because of communication and its impact on human decision making. A model is introduced where financial market performance has an impact on decision making through communication between people. On the other hand the sentiment created via communication has an impact on the financial market performance.

Keywords: synchronization; human decision making; complex system; decoupling; self-organized criticality; opinion formation; agent-based modeling

1. Introduction

Financial markets are generally thought of as random and noisy, beyond an understanding within an ordered framework. The elusive nature of the markets has been captured in theories like the efficient market hypothesis, basically considering price movements as random. Behind such a notion is the idea that price movements happening on a given day is a random phenomenon, basically taken from some probability distribution, describing in probabilistic terms what kind of event one should expect happening on a given day. The assumption seems natural and probably has its roots back in time, when people working in finance at the beginning of a work day, would turn on their radio, and register new financial events (again, the events assumed to be created by some higher instances). Such a descriptive framework also holds for more modern and general schema used in Finance, such as ARCH and GARCH models which are able to describe many of the stylized facts observed in empirical data. Socio-Finance [1] instead try to emphasize non-random human impact in the formation of prices in financial markets, in particular stressing the interaction taking place between people, either directly through communication or indirectly through the formation of asset prices which in turn will be seen to enable synchronization in decision making.

41

42 Synchronization in human decision making, and the impact it could have on financial asset
43 price formation, is not a well understood topic. The term is more known in economics, where
44 empirical studies have shown that international trade partners display synchronization in business
45 cycles. Déés and Zorell [2] find that economic integration fosters business cycle synchronization
46 across countries. Also similar production structure is found to enhance business cycle co-
47 movement. By contrast, they find it more difficult pinpoint a direct relationship between bilateral
48 financial linkages and output correlation. For other references that studies the topic of
49 synchronization and business cycles across countries see for example [3-5]. With the recent global
50 financial crisis questions have then been asked, as to what role financial market integration could
51 have on synchronization of business cycles across borders [6]? However, very little research has
52 been done on synchronization that is created endogenously by the financial markets themselves,
53 without necessarily an economic cause. Still, such phenomena could be relevant for both the onset
54 and continuation of financial crisis, see e.g. [7-8]. This leads naturally to the next question: could
55 synchronization endogenously created in financial markets, spill over into the economy and
56 thereby cause synchronization in business cycles across borders? A clear framework to understand
57 its dynamics, as well as conditions for onset of synchronization in decision making, therefore seems
58 highly relevant.

59 It should be noted that the term "synchronization" in this article covers a broader phenomenon
60 than "herding", a related term often used in the financial literature. In finance "herding" usually
61 refers to the simple case where people intentionally copy the behavior of others. It has been
62 suggested that it is rational to herd [9]. For instance; portfolio managers may mimic the actions of
63 other portfolio managers just in order to preserve reputation. It is easier to explain an eventuality
64 failure when everybody else also fails, than expose a failure due to bold forecasts and deviation
65 from the consensus. For a general review paper on herding see [10]
66 Here "synchronization" instead refer to the more general and complex case, where people don't
67 necessarily try to imitate the behavior of others, but rather by observing the same price behavior, or
68 through communication, end up in cases where a majority of a population synchronize in decision
69 making. From this point of view the synchronization described in this article, is maybe closer to the
70 idea of creation of conventions, put forward by Keynes [11].

71 Poledna et al. [7] highlights how the role of regulation policies could increase the amount of
72 synchronized buying and selling needed to achieve deleveraging, which in turn then could
73 destabilize the market. They discuss the new regulatory measures which have been proposed to
74 suppress such behavior, but it is not clear whether these measures really address the problem? In
75 addition they show how none of these policies are optimal for everyone: the risk neutral investors

76 would prefer the unregulated case with low maximum leverage, banks would prefer the perfect
77 hedging policy, and fund managers would prefer the unregulated case with high maximum
78 leverage. Aymanns and Georg [8] instead consider the case when banks choose similar investment
79 strategies, which in turn can make the financial system more vulnerable to common shocks. They
80 consider a simple financial system in which banks decide about their investment strategy based on
81 a private belief about the state of the world, and a social belief formed from observing the actions of
82 peers. They show how the probability that banks will synchronize their investment strategies
83 depends on the weighting between private and social belief.

84

85 In the following we will place the emphasis on the fact that price formation is the result of
86 human decision of buying or selling assets. Behind every trade is a human decision making, if not
87 by direct action of a human, then indirectly through the decision making made into the programs
88 that governs algorithmic trading made by computers. Socio-Finance [1] considers price formation as
89 a sociological phenomenon. It defines price formation to result from either direct or indirect human
90 interactions. Direct interaction covers the case where either individuals, or groups of individuals,
91 communicate directly and thereby influences mutual decision making with respect to trading
92 assets. At the first level, the individual level, indirect interaction covers the case where a trader
93 submits an order to buy or sell an asset. The resulting price movement of the asset is observed by
94 other traders, who in turn may change their decision making because of the price movement of the
95 asset caused by the initial trade. At the second level, the group level, indirect interaction covers the
96 case where whole markets have to wait on the outcome of pricing in other markets in order to find
97 the proper pricing.

98

99 **2. Three different ways synchronization can lead to contagion in financial markets**

100 2.1. Synchronization through indirect interaction of traders

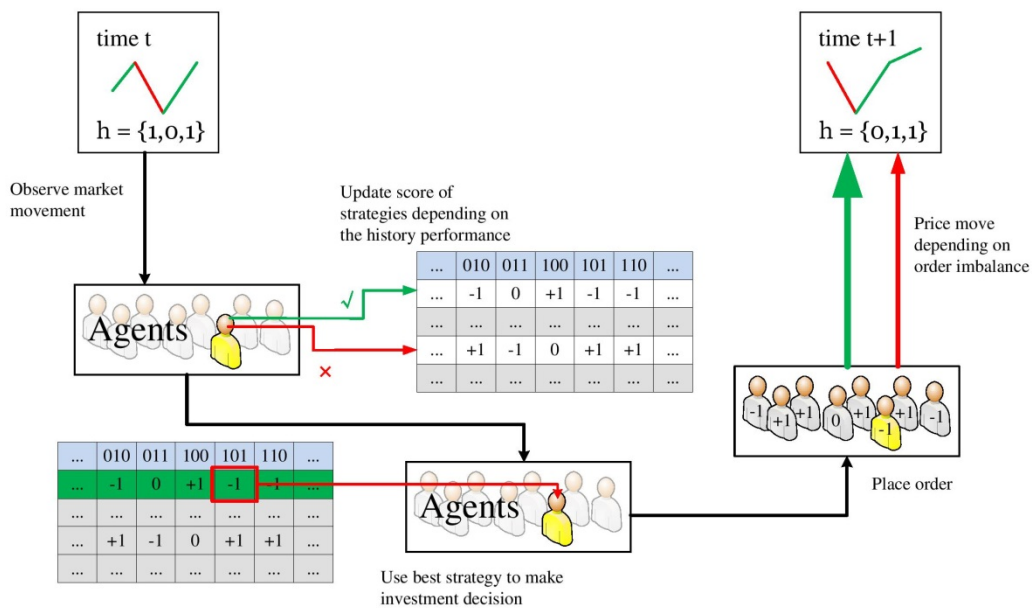
101 This section is divided into two parts: indirect interaction of market participants at the individual
102 level (section 2.1.1) and indirect interaction of market participants at the collective level (section
103 2.1.2).

104 2.1.1. Synchronization through indirect interaction of individuals: the first level

105 The deed of traders in the past, has a direct influence of the action of traders at the present. Past
106 buying and selling activities has led the market up to the present level, for which traders have to
107 decide whether now is an opportune moment to buy or sell. This applies to traders using technical
108 analysis, as well as traders instead using fundamental analysis. Technical analysis will give
109 different buy/sell signals depending on the exact price history made by traders in the past, whereas

110 fundamental analysis will make traders judge about whether the price level has become sufficient
 111 low in order to buy, or high enough in order to sell.

112 So, as traders take note of what happens in the market, and update their trading strategies
 113 accordingly, the new evaluations of their strategies will change their future prospects of how to
 114 trade in the market. Therefore as the markets change, the decision making of traders with respect to
 115 buying/selling change, and as they change, they thereby change the pricing of the market. This
 116 feedback loop is illustrated schematically in the figure below.



117
 118 **Figure 1.** Representation of the price dynamics in the Minority-Game [12] and the \$-Game [13].
 119 Agents first update scores of all their strategies depending on their ability to predict the market
 120 movement. After scores have been updated, each agent chooses the strategy which now has the
 121 highest score. Depending on the price history at that moment, this strategy determines which action
 122 a given agent will take. Finally, the sum of the actions of all agents determines the next price move:
 123 if positive, the price moves up, if negative, the price moves down. The figure is taken from [14].

124
 125 Under certain circumstances it can happen that traders inadvertently ends up in a state where their
 126 trading strategies “decouple” from the price history, so that over the next (evt. few) time step(s)
 127 their decision making become completely deterministic, independent of what happens next in the
 128 market. In order to illustrate this point, consider the table below which is one way of formalizing
 129 technical analysis trading strategies in a simple table form [12,13]. Considering for simplicity only

130 the direction of each of the last market moves, the table below predicts, for each possible price
131 history, the next move of the market. The table illustrates one technical analysis strategy that uses
132 the last three time periods in providing a prediction, and can easily be generalized to any number
133 of periods.

134

135 **Table 1.** Example of a strategy used in the Minority Game[12] and the $\$$ -Game[13]. Considering
136 only up (1) and down (0) price movements of the market, a strategy issues a prediction for each
137 given price history, here illustrated with price histories over the last $m=3$ days.

138

price history	prediction
0 0 0	1
0 0 1	-1
0 1 0	1
0 1 1	1
1 0 0	-1
1 0 1	-1
1 1 0	1
1 1 1	1

139

140 Consider now a given price history of the market, $\vec{\mu}(t) = (010)$, at time t , meaning that (as
141 illustrated in the figure below) three time periods ago the market went down, then up, and then
142 down. It should now be noted that *whatever* the price movement at the next time period $t+1$, the
143 strategy in table 1 will *always* predict to sell at time period $t+2$. Therefore we don't need to wait for
144 the market outcome at the next time step $t+1$ in order to know what the strategy will suggest
145 following that time step: it will always suggest selling at time $t+2$. That such kinds of dynamics in
146 the decision making of technical analysis strategies could be relevant for real market was suggested
147 in [15]. In the terminology of [15] the strategy in table 1 is called "one time step decoupled
148 conditioned on the price history $\vec{\mu} = (010)$ " and denoted $a_{\mu}^{decoupled}(t)$.

149 We can then divide trading strategies into two different classes: those coupled to the price history
 150 (i.e. conditioned on knowing $\vec{\mu}(t)$ one cannot know the prediction of $a_{\mu}^{coupled}(t)$ at time $t+2$ before
 151 knowing $\vec{\mu}(t+1)$), and those decoupled to the price history. Considering only the strategies
 152 actually used by the agents to trade at time t , the order imbalance, $A(t)$, can therefore be written:

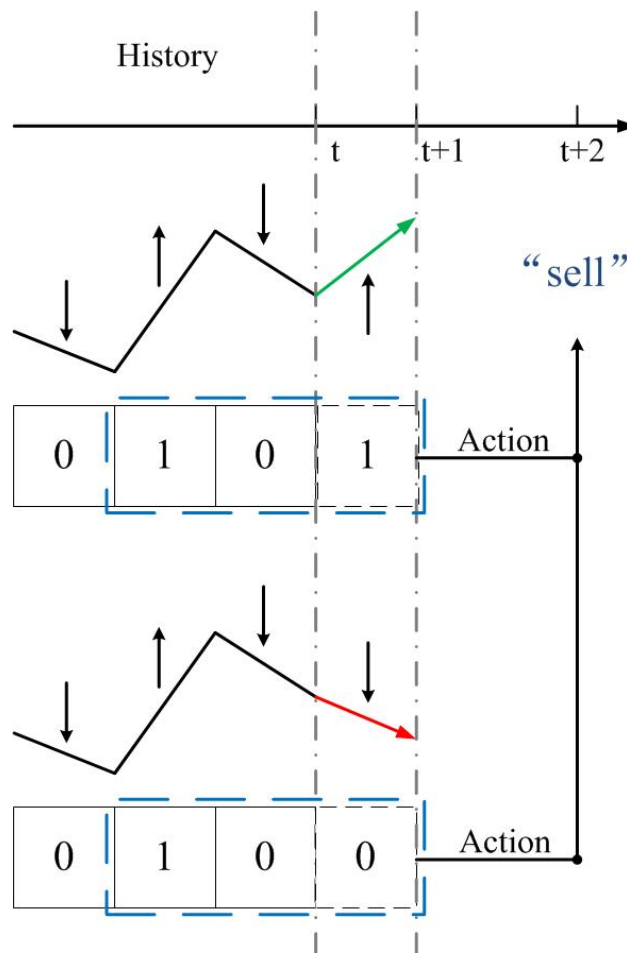
$$153 \quad A(t) \equiv A_{\mu}^{coupled}(t) + A_{\mu}^{decoupled}(t) \quad (1)$$

154 With $A_{\mu}^{coupled}(t) = \sum a_{\mu}^{coupled}(t)$ the sum over coupled strategies at time t and similarly for
 155 $A_{\mu}^{decoupled}(t) = \sum a_{\mu}^{decoupled}(t)$. The condition for *certain* predictability at time t , two time steps
 156 ahead is then:

$$157 \quad A_{\mu}^{decoupled}(t+2) > N/2. \quad (2)$$

158 If a majority of market participants hold decoupled strategies, this will ensure a deterministic future
 159 price movement of the market, independent of the choices made the minority that hold coupled
 160 strategies.

161



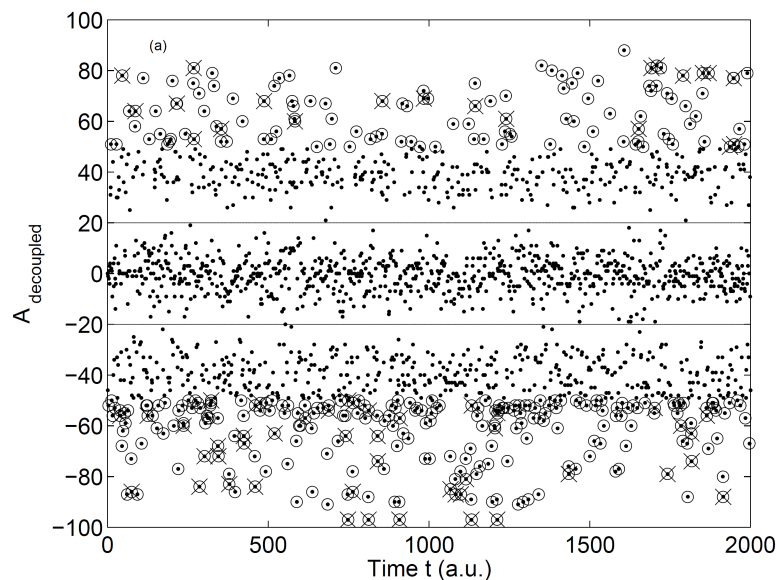
162

163 **Figure 2.** Representation of how the trading strategy in Table 1 decouples at time $t+2$ conditioned on
 164 the price history $\vec{\mu} = (010)$ at time t . Figure taken from [14].

165 The condition (2) gives the condition for synchronization to happen via indirect interaction of
166 traders through the price formation of an asset. Before considering synchronization in real markets
167 [14], one obviously first have to show its presence in models as well as in experiments. Indeed,
168 Figure 3 below proves synchronization via decoupling to be present in models like the Minority
169 Game, a somewhat surprising result since these types of games by definition don't support trend
170 following strategies. For more literature covering the situation with respect to synchronization in
171 experiments and markets, see [14-16].

172

173



174

175 **Figure 3.** An example of $A_{decoupled}$ defined from (1) as a function of time for a simulation of the
176 Minority Game. Circles indicate one-step days which are predictive with probability 1, crosses are
177 the subset of days starting a run of two or more consecutive on-step predictive days.

178

179 2.1.2. Synchronization through indirect interaction of groups of individuals: the second level

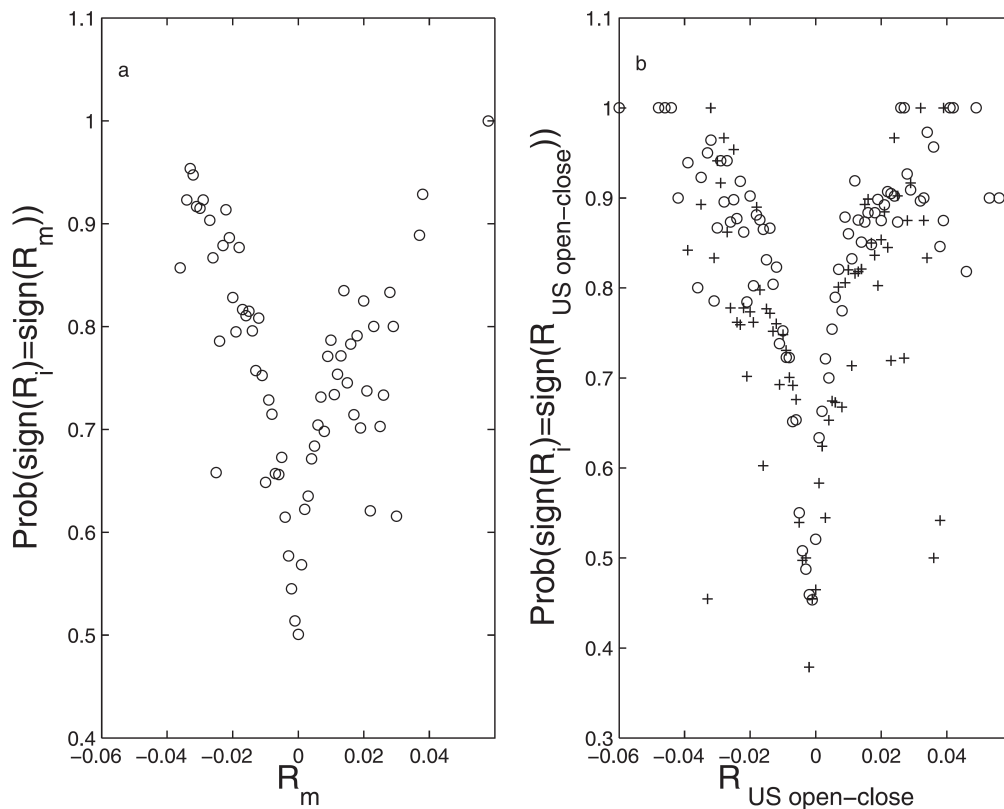
180 Having discussed how indirect interaction of individuals through financial indices can lead to
181 synchronization, let us next consider how the phenomenon can appear through indirect interaction
182 of groups of individuals. In this case we consider the reaction of one market to the pricing created
183 in another market. That is, we consider how one given market (i.e. a pool of traders) reacts to prior
184 price formation in another market (created by another pool of traders).

185 To illustrate this point, consider the figure below which shows how large price movements of large
186 capital stock indices, can have a particular impact on smaller capital stock indices. The figure

187 illustrates the effect of both a world market return (calculated as a weighted sum of returns of stock
 188 indices) and the US market return on the following price movements of individual stock indices.
 189 Using the open-close return of the U.S. stock market, gives a particular clear case to see a “large-
 190 move” impact across markets: since the Asian markets close before the opening of the U.S. markets,
 191 they should only be able to price in this information at their opening the following day. That is, one
 192 can consider the impact in the “close-open” of the Asian markets that should follow *after* an “open-
 193 close” of the US market. An eventual “large-move” U.S. open-close should therefore have a clear
 194 impact on the following close-open of the Asian markets. From the figure below this is indeed seen
 195 to be the case. On the contrary, the European markets are still open when the U.S. market opens up
 196 in the morning, so the European markets have access to part of the history of the open-close of the
 197 U.S. markets. An eventual “large-move” U.S. open-close would therefore still be expected to have
 198 an impact on the following close-open of the European markets, but with larger variation in the
 199 response than for the Asian markets, since part of the U.S. move would already be priced in when
 200 the European markets closed. This is seen to be the case.

201

202



203

204 **Figure 4.** Illustration of change blindness: a large world market return (fig a) or US market return
 205 (fig b) impacts a given stock exchange, whereas small returns have random impact. a) Conditional
 206 probability that the daily return R_i of a given country’s stock market index has the same sign as the

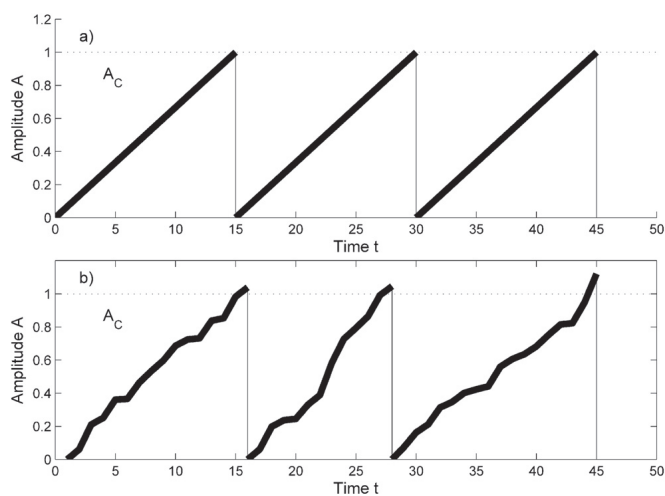
207 world market return. b) Conditional probability that the close-open (+: European markets; circles:
208 Asian markets) return R_i of a given country's stock market index following an U.S. open-close, has
209 the same sign as the U.S. open-close return. The figures were created using almost 9 years of daily
210 returns of 24 of the major stock markets worldwide. For more information see [17-18]

211

212 To see how synchronization can happen across markets, consider the illustration in Figure 4.a
213 below which shows three Integrate-And-Fire (IAF) oscillators with the same frequency over one
214 time period (or equivalently one IAF oscillator over three time periods). An IAF oscillator is
215 characterized by an accumulation (i.e. "Integrate") in amplitude $A(t)$ (e.g. "stress") over time t , up
216 to a certain point A_C , after which it discharges (i.e. "Fires"). The complexity of models of IAF
217 oscillators arise when the oscillators are coupled (i.e. the amplitude of one oscillator influences the
218 amplitude of other oscillators), and have different frequency (see Figure 4.b) and/or thresholds A_C^i .
219 Peskin [19] introduced IAF oscillators in neurobiology to describe the interactions of neurons, but
220 IAF oscillators have been introduced in many other contexts, for network studies of IAF oscillators
221 see e.g. Mirollo and Strogatz [20], Kuramoto [21], Bottani [22]. The link between certain, types of
222 integrate-and-fire oscillators are earthquake models has also been noted by e.g. Corral et al. [23].

223 As mentioned in [17], one can consider each financial market index as an IAF oscillator that
224 influences other market indices (i.e. other IAF oscillators). The impact, or "stress", from index i on
225 index j accumulates up to a certain point, after which it becomes priced-in. The justification for such
226 a behavior, can be seen from Figure 4, which shows that small price changes of index i has no
227 immediate influence on index j (but is assumed to accumulate over time), whereas large price
228 changes at index i , have an impact and thereby becomes priced-in at index j .

229



230

231

232 **Figure 5.** Illustration of an IAF oscillator. a) Illustrates the case where the amplitude $A(t)$ of an IAF
 233 oscillator integrates linearly in time until it reaches a critical value A_c , after which it discharges by
 234 setting $A(t) = 0$. The case in a) can be viewed as one IAF oscillating over three periods of time, or
 235 equivalently, three identical and uncoupled IAF oscillators oscillating over one period of time. b)
 236 An IAF oscillator with random frequency over three time periods, or equivalently, three different
 237 unit oscillators with random frequency over one time period. The figure is taken from [18].

238

239

240 This can be formalized in the following expression which expresses the set of stock market indices
 241 worldwide as a set of coupled IAF oscillators:

$$242 \quad R_i(t) = \frac{1}{N_i^*} \sum_{j \neq i}^N \alpha_{ij} \theta(|R_{ij}^{cum}(t-1)| > R_c) \times R_{ij}^{cum}(t-1) \beta_{ij} + \varphi_{ij}(t) \quad (3)$$

$$243 \quad R_{ij}^{cum}(t) = [1 - \theta(|R_{ij}^{cum}(t-1)| > R_c)] \times R_{ij}^{cum}(t-1) + R_j(t), \quad j \neq i \quad (4)$$

$$244 \quad \alpha_{ij} = 1 - \exp[-K_j/(K_i \gamma)]; \quad \beta_{ij} = \exp[-|z_i - z_j|/\tau] \quad (5)$$

245 In expression (3) $R_i(t)$ is the return of stock index j , which at time t receives a contribution from
 246 stock index j , whenever the “stress” R_{ij}^{cum} exceeds a certain threshold R_c . α_{ij} describes the coupling
 247 between the two stock indices, expressed via (5) in terms of the relative weight of capitalizations K_i .
 248 A large γ , $\gamma \gg 1$, corresponds to a network of the world’s indices with dominance of the index with
 249 the largest capitalization K_{max} . On the contrary a small γ , $\gamma \ll 1$, corresponds to a network of
 250 indices with equal strengths since α_{ij} then becomes independent of i, j . In addition it is assumed
 251 that countries which are geographically close, also have larger interdependence economically, as
 252 described by the coefficient β_{ij} , with $|z_i - z_j|$ the time zone difference of countries i, j . τ gives the
 253 scale over which this interdependence declines. Small τ , $\tau \ll 1$, then corresponds to a world where
 254 only indices in the same time zone are relevant for the pricing, whereas large τ , $\tau \gg 1$, describes a
 255 global influence in the pricing independent of the difference in time zone.

256 It is seen from (4), that it is the tensor R_{ij}^{cum} , that places the role of an IAF oscillator. Returns from
 257 index j , R_j , accumulates stress on index i by continuously adding to R_{ij}^{cum} , up to a certain point,
 258 $|R_{ij}^{cum}| > R_c$, after which the oscillator discharges, $R_{ij}^{cum} \rightarrow 0$, and the stress becomes priced-in via
 259 (3).

260 Once the IAF network is in a state of synchronization, it is possible to identify contagion effects
 261 throughout the network. One example is given in Figure 5 below, showing the propagation of a

262 large price movement taking place in the Japanese stock market on the 23/05/2013. For more
263 examples on real market data see [18]

264

265



266

267 **Figure 5.** "Price-quake". One of the main advantages of the non-linearity in the integrate-and-fire
268 oscillator model is that it enables a clear-cut identification of cause and effect; The figure shows one
269 example of a price-quake, following an initial minus 7% price movement on the Japanese stock
270 market on 23/05/2013. The figure is taken from [18].

271

272 2.2. Synchronization through direct interaction of traders

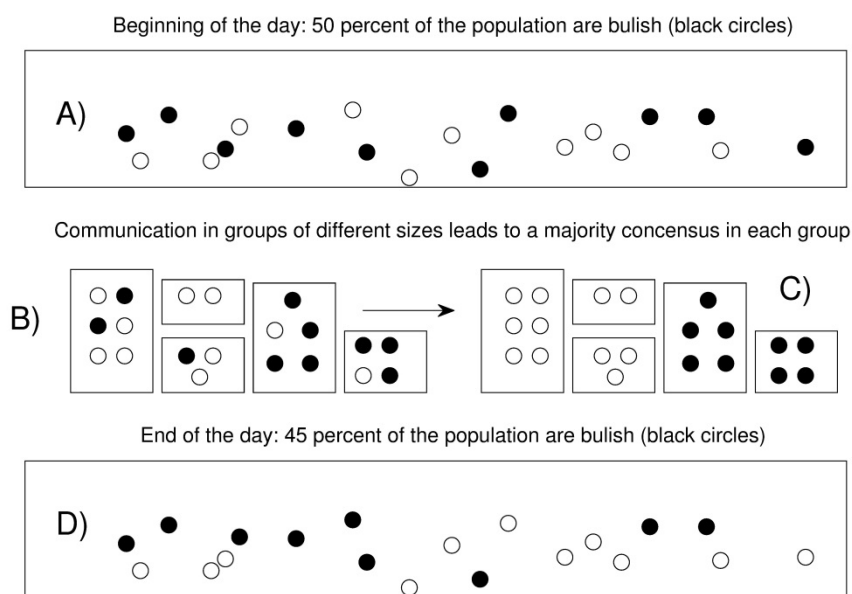
273 2.2.1. Synchronization through direct interaction of individuals and groups of individuals: the first
274 and second level.

275 Having discussed how synchronization can immerge through indirect interaction through financial
276 market indices of individuals, or groups of individuals, we now instead consider the case of direct
277 interaction, that is, how decision making is influenced by direct communication between people or
278 groups of people. The idea is to see how discussions among market participants, can influence their
279 decision making with respect to buying/selling assets, which in turn can influence the market
280 performance. On the other hand, we will show how the market performance itself can be a relevant
281 factor in the process of decision making, thereby creating another feedback loop between the
282 decision making of people and market performance.

283

284 To see how this can take place consider Figure 6.a below, which illustrate a population of market
285 participants with different views of the market, which we for simplicity will take either to be
286 positive, bullish, or negative, bearish. Figure 6.a illustrates an example where initially half the
287 population is bearish, the other half bullish. One could for example imagine a morning meeting

288 taking place in a major bank or brokerage house, and so at the beginning of the day, we let people
 289 meet and discuss around tables in groups of different sizes Figure 6.b. To illustrate how
 290 communication between people can influence their decision making, consider first the simple case
 291 where consensus making is determined by the majority opinion Figure 6.c. As seen in Figure 6.d, at
 292 the end of the day the opinion of the population has changed as a result of their meetings (direct
 293 interaction), with now only 45% of the population being bullish.



294

295 **Figure 6.** Changing the “bullishness” in a population via communications in subgroups. (a) At the
 296 beginning of a given day t a certain percentage $B(t)$ of bullishness. (b) During the day
 297 communication takes place in random subgroups of different sizes. Panel (c) illustrates the extreme
 298 case of complete polarization $m_{k,j} = \pm 1$ created by a majority rule in opinion. In general $m_{k,j} \approx j/k$
 299 corresponds to the neutral case where in average the opinion remains unchanged within a subgroup

300 of size k . (d) Due to the communication in different subgroups the “bullishness” at the end of the
301 day is different from the beginning of the day. The figure is taken from [25].

302

303 In the context of decision making with respect to trading assets in financial markets, it is natural to
304 assume that the market performance itself could influence the decision making of the market
305 participants, whereas this in turn could influence future market performance. In order to capture
306 such kinds of feedbacks, a model was suggested in [25]. The main idea is to let the market
307 performance influence the decision making, instead of the simple majority rule seen in Figure 6.b-c.
308 This is done by assuming a certain *probability* for a majority opinion to prevail. Thereby under
309 certain conditions, a minority could persuade a part of the majority to change their opinion. The
310 probability for a majority opinion to prevail, will depend on the market performance over the last
311 time period.

312 Specifically, let $B(t)$ denote the proportion of bullishness in a population at time t , the proportion of
313 bearishness is then $1 - B(t)$. For a given group of size k with j agents having a bullish opinion and k
314 $- j$ a bearish opinion, we let $m_{k,j}$ denote the transition probability for all (k) members to adopt the
315 bullish opinion, as a result of their meeting. After one update taking into account communications
316 in all groups of size k with j bullish agents, the new probability of finding an agent with a bullish
317 view in the population can therefore be written:

$$318 \quad \mathbf{B}(t + 1) = \mathbf{m}_{k,j}(t) \mathbf{C}_j^k \mathbf{B}^j [1 - \mathbf{B}(t)]^{k-j} \quad (6)$$

319 with

$$320 \quad \mathbf{C}_j^k \equiv \frac{k!}{j!(k-j)!} \quad (7)$$

321 It should be noted that the transition probabilities $\mathbf{m}_{k,j}(t)$ depend on time, since we assume that they
322 change as the market performance changes.

323 The link between communication and its impact on the markets, can now be taken into account by
324 assuming that the price return $r(t)$ changes whenever there is a change in the bullishness. It should
325 now be noted, that it is the *changes* in opinion that matters for the market performance, rather than
326 the *level* of a given opinion. Empirical data supporting this idea, can for example be found in [26].
327 The reasoning behind this, is that people having a positive view of the market would naturally
328 already hold long positions on the market. It is therefore rather when people change their opinion,
329 say becoming more negative about the market, or less bullish, that they will have the tendency to
330 sell. Assuming the return to be proportional to the percentage change in bullishness, $RB(t)$, as well
331 as economic news, $\varphi(t)$, the return $r(t)$ is given by

332
$$r(t) = \frac{RB(t)}{\mu} + \varphi(t), \mu > 0 \quad (7)$$

333 Here $\varphi(t)$ is a Gaussian distributed variable with mean 0 that described a standard deviation that
334 varies as a function of time depending on changes in sentiment:

335
$$\sigma(t) = \sigma_0 \exp\left(\frac{RB(t)}{\beta}\right), \sigma_0 > 0, \beta > 0. \quad (8)$$

336 The impact from the market performance on the decision making, can then be taking into account
337 by letting $m_{k,j}(t)$ depend on the market performance via:

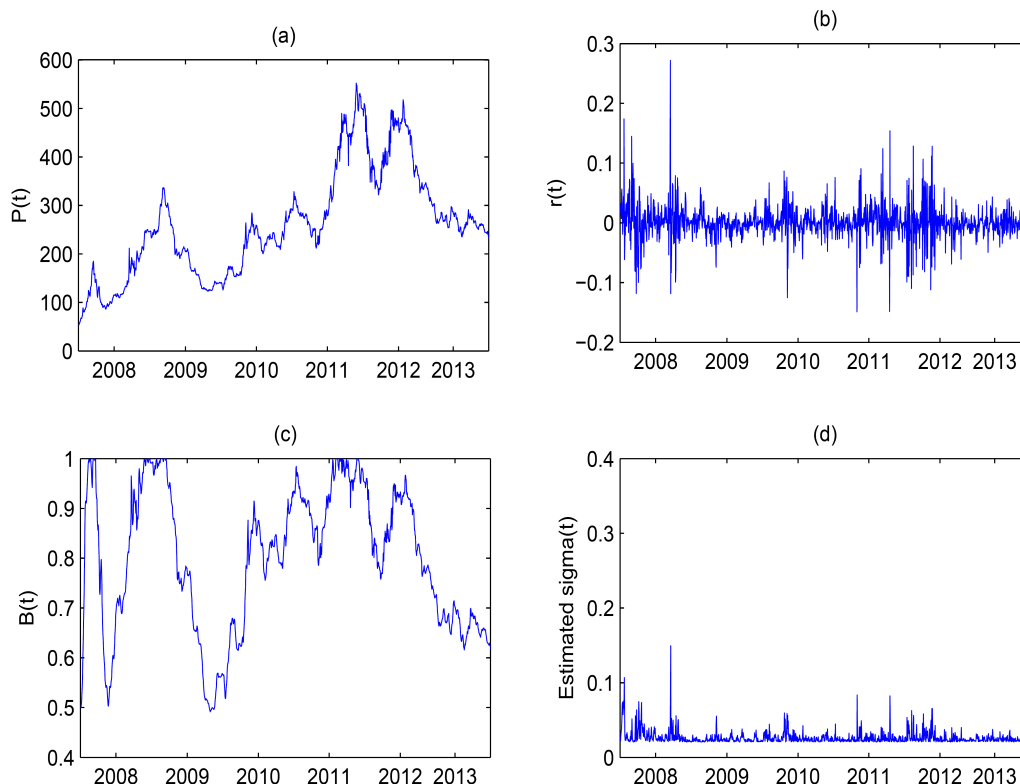
338
$$m_{k,j}(t) = m_{k,j} \exp\left(\frac{r(t)}{\alpha}\right), \alpha > 0, m_{k,j} \leq 1 \quad (9)$$

339 In this way the transition probabilities for a change of opinion, (9), depend directly on the market
340 return over the last time period. The reasoning for such dependence, is that if for example the
341 market had a dramatic downturn at the close yesterday, then in meetings the next morning, those
342 with a bearish view will be more likely to convince even a bullish majority about their point of
343 view.

344 Synchronization in the decision making due to communication between people, can now be studied
345 via for example tipping point analysis. Once extreme sentiment, $B=0,1$, has been created via
346 synchronization, this can be used to identify a tipping point of the market: when say $B \rightarrow 1$ any
347 further increase in B is limited, which in turn limits further price increases in the market. However,
348 any negative economic news, $\varphi(t)$, will then lead to a decrease in $B(t)$ through (7) and (9). The cases
349 of $B=0,1$ therefore acts as reflection points of the model, enabling thereby an identification of tipping
350 points of the price dynamics of the markets. One illustration of such tipping point dynamics in real
351 markets, can be seen in the figure below taken from [27]. In [27] maximum likelihood methods were
352 used to estimate the parameters of the model, after which an out-of-sample analysis was performed
353 on EUBanks index around the time of the financial crisis in 2008. As can be seen from Figure 7.a,c
354 prior peeks, $B \cong 1$, in the estimated sentiment indeed announce a tipping point in the performance
355 of the return of the index.

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362 **Figure 7.** This figure presents EUBanks index prices and returns, as well as the corresponding
 363 estimated conditional volatilities and bullishness proportions under the assumption of conditional
 364 Student-t distribution. (a) EUBanks index price $P(t)$, (b) EUBanks index returns $r(t)$, (c) Estimated
 365 bullishness proportions $B(t)$, (d) Estimated conditional volatilities $\sigma(t)$. The figure is taken from [27]

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368 3. Discussion

369 We have introduced three different models from Socio-Finance in order to capture three
 370 different pathways in which the market participants in financial markets could synchronize in
 371 decision making, and thereby create the route to contagious and volatile market phases. One
 372 pathway is caused when stock market indices, seen as a set of coupled integrate-and-fire oscillators,
 373 synchronize in frequency. Another pathway happens due to feedback mechanisms between market
 374 performance, and the use of certain (decoupled) trading strategies. Finally a third pathway could take
 375 place because of communication and its impact on human decision making.

376 Synchronization is a well-known phenomenon used in economics, to describe how trading
 377 partners can introduce synchronization in business cycles across international borders. With the

378 recent global financial crisis, one question is to what role financial market integration could have on
379 synchronization of business cycles across borders? Another question is whether synchronization
380 created endogenously in financial markets could spill over into the economy and thereby cause
381 synchronization in business cycles across borders? It should be noted, that very little research has
382 been done on synchronization that is created endogenously by the financial markets themselves,
383 without necessarily an economic cause. It is the hope of the authors that the present article could
384 help fuel awareness and interest on the topic.

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