ACCESS PRICING AND ENTRY IN THE POSTAL SECTOR

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Abstract

Postal markets are open to competitor for a long time. But, with a few exceptions, the competitors of the incumbent postal operator are currently active on the upstream segments of the market - preparation, collection, outward sorting and transport of mail products. With the further steps planned in the liberalization process, there are new opportunities to extend competition to the downstream segments of the market - the delivery of mails. In the future, two business model will be possible for the new postal operators: (1) access: where the firm perform the upstream operations and uses the incumbent’s delivery network and (2) bypass where the competing firm controls the entire supply chain and delivers mails with its own delivery network. These two options have a different impact on both the welfare and the profit of the historical operator. In particular, bypass raises severe concerns for the financing of the universal service obligations.

The choice between access and bypass depends on the entrant’s delivery cost relative to the cost of buying access to the incumbent operator (the access price). In this paper, we derive optimal -welfare maximizing- stamp and access prices for the incumbent operator when these prices have an impact on the delivery method chosen by the entrant. We show how prices should be re-balanced when the entry method is considered as endogenous i.e. affected by the incumbent’s prices.

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1 Introduction

This paper concentrates on the ongoing liberalization process of the postal sector in the European Union. It focuses on the entry of new postal operators on the downstream segments of the postal market (the delivery of mails). Competition in the postal sector raises a major concern for the financing of the universal service obligations (USO) imposed to the incumbent operators. USO includes the requirement to serve all customers (universality/ubiquity), the imposition of a geographically uniform tariff for a bundle of products, obligations in term of service quality (frequency of delivery, accessibility of contact points) and constraints on prices. It is commonly accepted that universal service obligations are associated with large fixed costs for the universal service provider (USP).

For the moment, the universal service obligations are (partially) financed by monopoly profits in the reserved areas. As these reserved areas will disappear, so will the associated monopoly profits (or at least part of them). In this case, the future of USO is no longer guaranteed and the financing of the USO becomes a major concern for both the regulator (or the State) and the USP. The extent of this problem will obviously depend on the scope of the USO and the importance of competition on the postal markets.

Maintaining the USO in a competitive market is thus a source of tension. To overcome this potential problem, proposals have been made to limit the scope of the USO and/or to limit competition to the upstream segments of the market. Moreover, the welfare impact of entry of competitors on the postal markets is not clear-cut. For example, Crew and Kleindorfer (2006) estimate that the impact on welfare of allowing downstream bypass is negative. Panzar (2005) shows that the development of both upstream and downstream competition does not conflict with the pursuit of public policies.

\footnote{Cazals et al. (1997), Cremer et al. (1997).}

\footnote{Like the US situation where the incumbent firm USPS maintains a monopoly position on the last mail delivery.}
(low prices, USO coverage) as long as piecemeal bypass (the possibility for mailers to buy access from a competitor) is not allowed. In his model, the development of E2E mail competition reduces the incumbent’s mail volume and therefore, the incumbent should charge a higher margin on its products to cover the fixed costs.

This paper concentrates on the impact of the incumbent’s pricing behavior on the entry of the competitors on the postal market. A potential competitor of the incumbent postal operator has different entry strategies: it can either deliver its mails using the existing delivery network of the incumbent operator (downstream access) or it can deliver its mails using its own delivery network (downstream bypass). If the competitor chooses downstream access, it performs itself all the upstream operations (collection, sorting, transport) and uses the incumbent’s delivery network for which it pays an access price. If the competitor chooses downstream bypass, it performs itself all the upstream and downstream operations.

In Sweden, City Mail chose the downstream bypass option and delivers mails with its own delivery network. But, City Mail has a limited geographical coverage. Sandd in the Netherlands has now a nationwide delivery network and achieves a market share of 8%. In the UK, UK-Mail (and many others) offers E2E mail services but the mails collected by UK-Mails are ultimately delivered by the incumbent operator, Royal Mail (downstream access).

This paper builds up on the literature on efficient access pricing in the postal sector (De Donder (2006), Billette de Villemeur et al. (2005), Laffont and Tirole (1994, 2000)). In the efficient access pricing approach, the incumbent’s stamp and access prices are derived by maximizing the total welfare while guaranteeing a non-negative profit for the firms. If USO obligations are imposed (or if there are fixed costs in the delivery activity), the access price paid by the entrant to the incumbent operator is equal to the incumbent’s marginal cost of delivery plus a mark-up. This mark-up aims at covering
part of the fixed costs associated with the incumbent’s USO. It can be decomposed into a ‘Ramsey term’ and a ‘displacement term’. For each product, including access, the Ramsey term is inversely related to the product’s price elasticity. Products for which the demand is highly sensitive to prices are charged a lower mark-up than those who are relatively less price sensitive. The displacement term is the product of the incumbent’s margin on its E2E products and the displacement ratio who measures the substituability between the incumbent’s and the entrant’s products. If the entrant attracts a large fraction of the incumbent’s consumers (the displacement ratio is high), competition creates serious concerns for the USO financing. Therefore, the regulator will set a high access charge to levy a large contribution to the USO financing from the entrant. Conversely, if the entrant offers innovative products and attract few consumers from the incumbent but rather attracts new consumers, its contribution to the USO financing will be lower.\(^3\)

All these papers consider as given the entrant’s delivery method -access or bypass. In this paper, we consider this choice as endogenous. The choice of one of these strategies depends (1) on the entrant’s technology and in particular its delivery costs and (2) on the incumbent’s products and access prices. Our objective in this paper is to derive efficient stamp and access prices when the entrant’s delivery method is affected by those prices.

**Overview of the results.**

In this paper, we start by deriving the efficient access and stamp prices in the case where the entrant buys access to the incumbent’s delivery network and in the case in which it bypass and builds up its own delivery network. We start our analysis by considering that the incumbent’s stamp prices depend on the delivery region (non-uniform tariff). In the case of downstream access, the access price is equal to delivery cost plus a Ramsey term plus a

\(^3\)Displacement ratios are likely to be high in the postal sector. For example De Donder et al. (2006) calibrate a model with displacement ratios of 0.75 and 0.9, meaning that three quarter (or 9 over 10) of the mails treated by the competitors are displaced from the incumbent.
displacement term. Under bypass, there are two modifications in prices: (1) the tariff is a rebalanced and the incumbent is relatively more aggressive on the urban market where it faces competition. (2) Because the USP loses access receipts, there is an overall increase of all its prices to cover the fixed costs associated with the USO.

Then, we compute the efficient delivery choice for the entrant. One needs to distinguish between the \textit{technologically efficient delivery method} and the \textit{socially efficient delivery method}. On the basis of costs, the entrant should by-pass the incumbent as long as its marginal delivery cost is lower than the marginal delivery cost of the incumbent. However, taking into account the USO and the fact that the incumbent needs to cover the fixed cost of maintaining his delivery network, the socially efficient delivery method involves access even when the entrant has a lower delivery cost. This result shows that an entrant who chooses his delivery method on the basis of costs will bypass for a range of parameters for which access is socially efficient. Hence, \textit{excess bypass can arise on the market, but excess access never occurs}. Furthermore, it is interesting to note that bypass may not be the efficient delivery method when the delivery cost of the entrant is too low. In that case, competition may drive the profits of the incumbent below the cost of USO, and hence lead the regulator to prefer access.

We then consider the problem faced by a regulator who cannot choose the delivery method of the entrant, and must take the entrant’s incentive as a new constraint in his maximization problem. We then show that the \textit{regulator’s choice will be aligned with technological efficiency}: the regulator promotes access when the incumbent has a lower delivery cost, and bypass when the entrant has a lower delivery cost.

When a uniform tariff is imposed on the USP, the incumbent postal operator has less freedom to set prices and it therefore has an impact on the entry strategy of the competitor. As urban mail price increases, the entrant is able to capture a larger fraction of the urban mail demand with a given price. In
other words, the displacement ratio is higher. As a consequence, the efficient access price increases which makes bypass more attractive for the entrant. Then, inducing the efficient choice of access requires more distortion in the prices than in the case of non-uniform tariff. This means that the cost in term of welfare of having an efficient delivery method is higher.

We also consider a situation of incomplete information, when the regulator and the USP only know the prior distribution of the entrant’s delivery costs but not its realization. This uncertainty in costs translates into an uncertainty in the choice of a delivery method. The probability of entry with bypass is endogenous and it depends on the access and stamp prices. The regulator then faces a trade-off between promoting efficiency, that is reducing the probability of bypass, which requires a low access price and USO financing which instead requires a high access price. We show that uncertainty on the entrant’s delivery cost could induce the entrant to bypass with a positive probability, even if it is not ex-post efficient.

Our approach differs from the Efficient Component Pricing Rule (ECPR) which also takes the market structure as endogenous. In the ECPR approach (Armstrong (2001) for example), it is efficient to have one producer serving the entire market segment. The ECPR pricing rule is then designed to select the most efficient producer. By setting the access price equal to the incumbent’s opportunity cost i.e. its retail price minus its cost, the ECPR gives the right incentive to the entrants. They enter the market only if they are more efficient than the incumbent operator. In our approach, the prices are not designed to select the most efficient producer but to maximize the welfare taking into account that the regulator does not control the choice of the delivery method by the entrant.

The contribution of this paper is to analyze the impact of pricing

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4 This part of the paper is closely related to Dam and Gautier (2006) who develop Ramsey pricing formulas that applies when the entry on the market is endogenous.

5 ECPR and efficient prices will only coincide in exceptional circumstances. See for example Laffont and Tirole, 2000, Armstrong, Doyle and Vickers, 1996.
on the entry strategy of the competitor i.e. how prices should be adapted to take into account their impact on the entry behavior of the competitors. By doing so, we neglect other issues like the reform of the USO. Clearly, relaxing some of the USO constraints is another possible way to overcome the problem of USO financing in a competitive market (see Crew and Kleindorfer 2006).

2 Model

There are two postal operators on the market: an incumbent postal operator -we call it firm 1- and an entrant -firm 2-. By assumption, USO are imposed to firm 1 only and the regulatory regime is an asymmetric one: firm 1 is fully regulated while firm 2 is not. However, we will assume that firm 2 behaves competitively.

Mails are delivered in two delivery zones: a high density region (urban) and a low density region (rural). Delivery costs depend on the population density and differ in the two regions.

Each postal operator offers end-to-end (E2E) mails to consumers. Firm 1 delivers mails to both regions. This ubiquity constraint is part of the USO imposed to the incumbent. Firm 2 serves only the most profitable, urban, region. In the sequel, we use indices $i = 1, 2$ to refer to firms and exponents $k = u, r$ to refer to the delivery zone. The mail products of the two firms are differentiated. For example, the incumbent operator offers $J+1$ E2E mails to the customers while the entrant offers mail services with a lower frequency of delivery. Customers view the two products as imperfect substitutes. Moreover, we consider that the degree of product differentiation is not affected by the method chosen for delivery.

There are two types of costs associated with the production of E2E mails: an upstream and a downstream (delivery) costs. We represent by $c_i$, the unit

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6Sand and City Mail deliver letters twice a week. Most of the mail providers that choose access offer a day definite mail delivery, 2 or 3 days after the mail collection.
cost of all the upstream operations (collection, sorting, transport,....) for firm \(i = 1, 2\). This upstream cost is independent of the delivery region. Because of the universal service obligations imposed to firm 1, the two firms have a different cost structure for their delivery activities. For the universal service provider, delivery costs are mainly fixed costs. We denote this fixed cost by \(F\).\(^7\) In addition, there is a unit cost of \(d^u_i\) (resp. \(d^r_i\)) per mail delivered in the urban (resp. rural) area. Delivery costs are higher in the rural region: \(d^r_i > d^u_i\). Firm 2 has a more flexible cost structure with no fixed cost and only variable costs. For the entrant, the unit cost of delivering one mail in the urban region is \(d^u_2\). The entrant can avoid this delivery cost by buying access to the delivery network of firm 1. In this case, it pays a per-unit access charge denoted by \(\alpha^u\) to firm 1 and firm 1 supports the delivery cost \(d^u_1\).

The net surplus of a representative consumer who sends \(x^k_i\) mails to zone \(k\) with the incumbent (\(i = 1\)) and \(x^u_2\) mails to the urban zone with the entrant is:

\[
U(x^u_1, x^r_1, x^u_2) - p^u_1x^u_1 - p^r_1x^r_1 - p^u_2x^u_2
\]

where the \(p^k_i\) are the prices charged by firm \(i\) for their E2E mails delivered in zone \(k\).

The maximization of this surplus function gives the demand for each type of mail \(x^k_i\). We will make the following assumptions on the demand functions:

1. \(\frac{\partial x^u_1}{\partial p^u_1} \leq 0\) and \(\frac{\partial x^r_1}{\partial p^r_1} \leq 0\)

2. \(\frac{\partial x^u_2}{\partial p^u_1} = 0\) and \(\frac{\partial x^u_2}{\partial p^u_2} = 0\)

Part 1 means that consumers give a positive value to the ubiquity of the service offered by the USP. Urban and rural mails offered by firm 1 are thus complements. In addition, the demand functions satisfies the standard following properties: \(\frac{\partial x^k_i}{\partial p^j_i} < 0, \frac{\partial x^u_i}{\partial p^u_j} > 0\) and \(\left|\frac{\partial x^u_i}{\partial p^u_j}\right| \geq \frac{\partial x^u_i}{\partial p^u_j}\).

In the sequel, we use elasticities in the pricing formulas. These elasticities are defined as follow:

\(^7\)or \(F\) represents all the costs associated with the USO.
Definition 2.1

1. The direct price elasticity (in absolute value) of a product sold by firm $i$ in region $k$ is: $\eta^k_i = -\frac{dx^k_i}{dp^k_i} \frac{p^k_i}{x^k_i}$.

2. The cross price elasticity of a product sold by firm $i$ on the urban market is, for $i, j = 1, 2$: $\eta^{uu}_{ij} = \frac{dx^u_i}{dp^u_j} \frac{p^u_j}{x^u_i}$.

3. The intra-brand price elasticities for firm 1 are: $\eta^{ur}_{1} = \frac{dx^u_1}{dp^r_1} \frac{p^r_1}{x^u_1}$ and $\eta^{ru}_{1} = \frac{dx^r_1}{dp^u_1} \frac{p^u_1}{x^r_1}$.

Consistent with our assumptions, we have positive cross price elasticities and negative intra-brand price elasticities.

The total welfare is the sum of the consumer’s and producers’ surplus:

$$W = U(x^u_1, x^r_1, x^u_2) - (c_1 + d^u_1)x^u_1 - (c_1 + d^r_1)x^r_1 - (c_2 + \theta d^u_1 + (1 - \theta)d^u_2)x^u_2 - F$$ (2.1)

where $\theta$ is a dummy variable that has a value of one if firm 2 chooses to buy access to deliver its mails and equals to zero if it chooses bypass. The aim of the regulator is to set the stamp prices $p^u_1$, $p^r_1$ and the access price $\alpha^u$ in order to maximize the total welfare $W$. We will consider sequentially two cases. In the first one, the stamp price for mails to the urban and the rural area can be different. In the second one, a geographically uniform tariff is imposed: $p^u_1 = p^r_1 = p^u_2$.

Firm 2 behaves as a competitive fringe. The competitive fringe assumption means that its product is sold at marginal cost. Since this cost depends on the delivery method, the stamp price charged by firm 2 is for its urban mail is:

$$p^u_2 = c_2 + \alpha^u \quad \text{if firm 2 chooses access},$$
$$p^u_2 = c_2 + d^u_2 \quad \text{if firm 2 chooses bypass}.$$

With this marginal cost pricing rule, the profit of firm 2 is in any case equals to zero. We therefore assume that firm 2 chooses the delivery technology with the lowest cost, that is access if $\alpha^u \leq d^u_2$ and bypass otherwise.


3 Non-uniform pricing.

In this section, we derive the welfare maximizing prices when the regulator can set a different stamp prices for mails delivered in the urban and the rural regions. For convenience, the technical analysis is relegated to appendix A.

3.1 Access

Suppose that firm 2 uses firm 1 delivery network for which it pays an access fee of $\alpha_u$ per mail distributed. If firm 2 chooses access, the welfare is:

$$W_a = U(x_1^u, x_1^r, x_2^u) - (c_1 + d_1^u)x_1^u - (c_1 + d_1^r)x_1^r - (c_2 + d_1^u)x_2^u - F$$

The regulator selects the prices that maximize the welfare and that guarantee to firm 1 a non-negative profit i.e. firm 1 is able to cover its costs (including the fixed cost of the USO) with its receipts from E2E mails and from access. This zero profit constraint is:

$$\Pi_1^a = (p_1^u - c_1 - d_1^u)x_1^u + (p_1^r - c_1 - d_1^r)x_1^r + (\alpha_u - d_1^u)x_2^u - F \geq 0 \quad (3.2)$$

Firm 2 sells its mail product at marginal cost and charge a price equals to:

$$p_2^u = c_2 + \alpha_u \Rightarrow \Pi_2 = 0 \quad (3.3)$$

The regulator’s objective is to find the stamp prices for the incumbent and the access price that maximize the welfare subject to the constraint (3.2). We denote by $\lambda$ the Lagrange multiplier of the zero profit constraint for firm 1. (3.3) implies that the derivative of the demand $x_1^k$ with respect to $\alpha_k$ is equal to the derivative of $x_1^k$ with respect to $p_2^k$. The first order conditions to
(1 + \lambda) \left( (p_1^u - c_1 - d_1^u) \frac{\partial x_1^u}{\partial p_1^u} + (p_r^r - c_1 - d_1^r) \frac{\partial x_1^r}{\partial p_1^r} + (\alpha^u - d_1^u) \frac{\partial x_2^u}{\partial p_1^u} \right) + \lambda x_1^u = 0 \tag{3.4}

(1 + \lambda) \left( (p_1^u - c_1 - d_1^u) \frac{\partial x_1^u}{\partial p_1^r} + (p_r^r - c_1 - d_1^r) \frac{\partial x_1^r}{\partial p_1^r} \right) + \lambda x_1^r = 0 \tag{3.5}

(1 + \lambda) \left( (p_1^u - c_1 - d_1^u) \frac{\partial x_1^u}{\partial p_2^u} + (\alpha^u - d_1^u) \frac{\partial x_2^u}{\partial p_2^u} \right) + \lambda x_2^u = 0 \tag{3.6}

This type of first order conditions are standard in efficient access pricing problems (see for example De Donder, 2006). Rearranging the terms in the first order conditions, we can express the prices as the sum of three terms: price = marginal cost + a Ramsey term + a displacement term. That is:

\[ \alpha^u = d_1^u + \frac{\lambda}{1 + \lambda} \frac{p_2^u}{\eta_2^u} + (p_1^u - c_1 - d_1^u)\sigma^u \tag{3.7} \]

where \( \eta_2^u \) is the price elasticity of urban mail of firm 2 (in absolute value) and \( \sigma^u \in [0, 1] \) is the displacement ratio: \( \sigma^u = -\frac{dx^u_1/\partial p^u_2}{dx^u_2/\partial p^u_2} \).

Similarly, the stamp prices for the incumbent’s mails are:

\[ p_1^u = c_1 + d_1^u + \frac{\lambda}{1 + \lambda} \frac{p_1^u}{\eta_1^u} + \bar{\sigma}^u(\alpha^u - d_1^u) + \sigma^u(p_r^r - c_1 - d_1^r), \tag{3.8} \]

\[ p_r^r = c_1 + d_1^r + \frac{\lambda}{1 + \lambda} \frac{p_2^r}{\eta_2^r} + \sigma^u(p_1^u - c_1 - d_1^u), \tag{3.9} \]

where \( \eta_1^r \) is the price elasticity of mails sent to region k by firm 1 and \( \bar{\sigma}^u \in [0, 1] = -\frac{dx^u_1/\partial p^u_1}{dx^u_1/\partial p^u_1} \), \( \sigma^u \in [-1, 0] = -\frac{dx^u_1/\partial p^u_1}{dx^u_1/\partial p^u_1} \) and \( \sigma^u \in [-1, 0] = -\frac{dx^u_1/\partial p^u_1}{dx^u_1/\partial p^u_1} \).

Solving this system, the efficient prices can be expressed as:

\[ L_1^u \equiv \frac{p_1^u - c_1 - d_1^u}{p_1^u} = \frac{\lambda}{1 + \lambda} \left( \frac{1}{\eta_1^u} + \gamma_1^u \right), \tag{3.10} \]
where $\hat{\eta}^u = \frac{\eta^u - \eta^u \eta^r}{\eta^u + \eta^r}$ and $\gamma^u > 0$. Similarly,

$$L^r_1 \equiv \frac{p^r_1 - c_1 - d^r_1}{p^r_1} = \frac{\lambda}{1 + \lambda} \left( \frac{1}{\hat{\eta}^r_1 + \gamma^r_1} \right). \tag{3.11}$$

where $\hat{\eta}^r_1 = \frac{\eta^r_1 - \eta^r_1 \eta^u}{\eta^r_1 + \eta^u}$ and $\gamma^r_1 < 0$.

To start the discussion of these optimal prices, it is convenient to recall that, in the absence of competition, the optimal stamp price in region $k$ would be set at a level such that $p^k_1 - c_1 - d^k_1 = \frac{\lambda}{1 + \lambda} \frac{1}{\hat{\eta}^k_1}$. In other words, the optimal prices for a monopolist are inversely related to the so-called super-elasticities of its products.\(^8\) Because urban and rural mails are complements, we have $\hat{\eta}^u_1 > \eta^u_1$.

How are prices modified with the presence of a competitor buying access? There are two main modifications. First, if entry is not neutral with respect to the incumbent’s profit i.e. if the access receipts less than compensate the lost receipts from the customers, there is an overall increase in prices. This change is captured by an increase in the value of the Lagrange multiplier $\lambda$. Second, the tariff is rebalanced. This change is captured by the '$\gamma$' terms in the above expressions. This '$\gamma$' term is positive on the urban market and negative in the rural market. The displacement ratios explain these modifications in the prices.

In the sequel, we denote by $p^k_1$ and $\alpha^*$, the optimal prices that the regulator applies if the entrant buys access.

### 3.2 Bypass

Now suppose that firm 2 bypasses the incumbent’s delivery network. The regulator selects the prices $p^k_1$ in order to maximize:

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\(^8\)Laffont and Tirole, 2000.
\[ W^b = U(x_1^u, x_1^r, x_2^u) - (c_1 + d_1^u)x_1^u - (c_1 + d_1^r)x_1^r - (c_2 + d_2^u)x_2^u - F \]

subject to:

\[ \Pi_1^b = (p_1^u - c_1 - d_1^u)x_1^u + (p_1^r - c_1 - d_1^r)x_1^r - F \geq 0 \quad (3.12) \]

Firm 2 sells its mail product at marginal price which leads to:

\[ p_2^u = c_2 + d_2^u \Rightarrow \Pi_2 = 0 \quad (3.13) \]

In the case of bypass, there is (by definition) no access receipts and therefore the value of \( \alpha^u \) is not meaningful in this case. The first order conditions can be expressed as:

\[ p_1^u = c_1 + d_1^u + \frac{\lambda}{1 + \lambda \eta_1^u} p_1^u + \sigma^ur(p_1^r - c_1 - d_1^r), \quad (3.14) \]

\[ p_1^r = c_1 + d_1^r + \frac{\lambda}{1 + \lambda \eta_1^r} p_1^r + \sigma^ru(p_1^u - c_1 - d_1^u). \quad (3.15) \]

If we compare prices under bypass with those that are applied under access, there are two main differences: (1) the prices are re-balanced: urban mail for which firm 1 faces competition is relatively cheaper in the case of bypass than in the case of access. Comparing (3.8) and (3.14), the positive displacement term has disappeared in the case of bypass. (2) There is an overall increase in stamp prices. Since firm 1 does not collect any access receipts, the financial burden of the USO is supported by the mark-up on its product only. As a consequence, prices should increase (i.e. \( \lambda \) increases).

Solving the system, the prices can be inversely related to the superelas-
ticity of the products:

$$L_1^k = p_1^k - c_1 - d_1^k = \frac{\lambda}{1 + \lambda \tilde{\eta}_1^k} \frac{1 + \lambda \eta_1^k}{p_1^k}$$  \hspace{1cm} (3.16)$$

Under bypass, the price structure is similar to the monopoly prices but the overall level of prices is higher since the firm faces a stronger financial constraint. In other words, the firm should raise its prices to compensate the lost receipts on the urban market due to the presence of the competitor.

Under bypass, it is possible that the incumbent does not manage to break events. If, the entrant’s price is low enough and it captures large mail volumes on the urban market and if, even the profit-maximizing prices for the incumbent are insufficient to allow break-events, then graveyard spiral takes place.\(^9\) In this case, it is not possible to sustain the USO.

In the sequel, we denote the prices under bypass as \(p_{1}^{kb}\).

### 3.3 Access vs. Bypass

We now compare welfare under bypass and access, \(W^a\) and \(W^b\) when the regulator controls the delivery decision of the entrant. The idea is to derive the welfare maximizing delivery method. We establish that:

**Proposition 3.1** There exists a cut-off point \(d^* < d_1^i\) such that \(W^a \geq W^b\) for all \(d_2^u \geq d^*\).

**Proof** We first show that \(W^a \geq W^b\) for any \(d_2^u \geq d_1^i\) (with strict inequality if \(d_2^u > d_1^i\)). The argument is a revealed-preference argument. In a model with access, the regulator could replicate the bypass prices by setting \(\alpha^a = d_2^u, p_1^{ua} = p_1^{ab}, p_1^{ra} = p_1^{rb}\). This would result in a welfare level \(W^a\). As long as \(d_2^u \geq d_1^i, W^a \geq W^b\). Furthermore, as \(\alpha \geq d_1^i, \Pi_1^a = \Pi_1^b + (\alpha - d_1^i)x_2^u \geq \Pi_1^b = 0\). So the choice \(\alpha = d_2^u, p_1^{ua} = p_1^{ab}, p_1^{ra} = p_1^{rb}\) is a feasible choice for the regulator. Hence \(W^a \geq W^a \geq W^b\).

Suppose $d_u^2 = d_1^1$. We can still show that $W^a > W^b$. The argument is that the optimal choice of $\alpha$ must involve $\alpha^* > d_1^u$ (see the equation characterizing the optimal choice of $\alpha$). Intuitively, the regulator prefers that the incumbent make a positive profit on the market where prices are not distorted, rather than raise prices to make sure that the profit constraint is satisfied.

As $W^a$ and $W^b$ are continuous functions of $d_u^2$ and $d_1^u$, this shows that there exists $\varepsilon > 0$ such that $W^a \geq W^b$ for all $d_1^u \geq d_2^u - \varepsilon$.

This proposition shows that as long as the entrant’s marginal cost of delivery is higher than the incumbent’s marginal cost of delivery in the urban area, access is the efficient (welfare maximizing) delivery method. If the two firms have identical delivery costs, the regulator still prefers access to bypass, since it raises money to finance the USO with access but not with bypass. By continuity of the welfare functions, this must hold also for $d_1^u \geq d_2^u - \varepsilon$. Hence, we observe that there exists a range of delivery costs for the entrant where the entrant is technologically efficient ($d_2^u < d_1^u$), but the regulator would prefer that the entrant buy access from the technologically inefficient operator.

A couple of remarks should be made. First, a key assumption for the result of proposition 3.1 is that the quality of the entrant’s product is independent of the delivery technology chosen. The two firms sell different products but the entrant sells the same product with the two delivery methods. In other words, it is assumed that the entrant cannot increase its product quality by controlling the whole supply chain. Of course, if it was not the case the welfare under bypass would be higher and the parameter space under which bypass is efficient would increase. Second, we take as granted that the USO is financed by the USP’s profits and the access receipts. We then neglect other financing methods like the compensation fund (a method that is explicitly provided in French postal law but not yet used). Third, we implicitly assume that upstream competition is welfare enhancing. This is
in fact the case if the entrant’s product is sufficiently differentiated and/or the upstream cost $c_2$ is not too big compared to $c_1$.

Notice that Proposition 3.1 is silent on the relation between access and bypass when the delivery cost of the entrant is below $d^*$. Intuitively, one would expect that bypass is preferred to access when the technological advantage of the entrant (measured by the difference $d_1^u - d_2^u$) is high. This is not necessarily the case, because bypass would then induce a very low price $p_{2}^b$, hence a high level of competition on the urban market which may prevent the operator from recovering its cost. Hence, the regulator may prefer to force access even though delivery costs of the entrant are very low, in order to guarantee nonnegative profits to the USP. We illustrate this reasoning with the following example:

**Example 3.1** Suppose that there only two urban markets, with utility $U(x_1, x_2) = x_1 + x_2 - \frac{1}{2}x_1^2 - \frac{1}{2}x_2^2 - \beta x_1 x_2$. Let the upstream costs be given by $c_1 = c_2 = 0$, the downstream costs be given by $d_1$ and $d_2$.

Under access, it is easy to see that the optimal prices are given by

$$p_1^a = \alpha^* = \frac{1 + d_1 - \sqrt{(1 + d_1)^2 - 2(2d_1 + F(1 + \beta))}}{2}$$

Under bypass, the optimal price is given by

$$p_1^b = \frac{1 - \beta + \beta d_2 + d_1 - \sqrt{(1 - \beta + \beta d_2 + d_1)^2 - 4(d_1(1 - \beta + \beta d_2) + F(1 - \beta^2))}}{2}$$

The next graph plots the welfare levels under access and bypass, $W^a$ and $W^b$ as a function of the delivery cost of the entrant, $d_2$ for $\beta = 1/2, d_1 = 1/2$ and $F = 1/100$.

The dashed line corresponds to welfare under access. This is independent of the delivery cost of the entrant, and under our parameter values, the incumbent can always cover the fixed cost under access. The solid line corre-
It is easy to check that if $d_2 < 0.3464$, the incumbent cannot cover his fixed cost, so bypass becomes infeasible. However, bypass is the preferred delivery method for any value $0.3464 \leq d_2 < 0.498$, and access is again preferred for $d_2 \geq 0.498$.

3.4 Constrained access

We now turn to the key issue of the paper. Suppose that the regulator cannot choose the delivery method of the entrant, but is constrained by the decision of the entrant. In that case, suppose that firm 2 chooses access whenever $\alpha^* \leq d_2^u$. Consequently, for all the values of $d_2^u \in [d^*, \alpha^*]$, the firm chooses bypass while access is socially preferred. This impact of

---

10 In this simple example, welfare under bypass is monotonically decreasing in $d_2$. However, this need not be the case in general.

11 In fact, given our assumption that the entrant behaves as a competitive fringe, it will never make any profit irrespective of its delivery cost. However, it seems natural to suppose that if the entrant is faced with two different costs, it will choose the delivery method with the lowest cost.
prices on the delivery method should be incorporated in the design of the optimal prices. In the next subsection, we then derive a constrained access solution where the regulator induces the efficient technological choice by the entrant. In the constrained access case, the regulator maximizes the welfare $W^a$ under the additional constraint that $\alpha^u \leq d^u_2$. This constraint aims at inducing an efficient technological choice by firm 2. When this constraint binds, the efficient stamp prices for the incumbent operator are:

\[
\frac{p^u_1 - c_1 - d^u_2}{p^u_1} = \frac{\lambda}{1 + \lambda \hat{\gamma}^u_1} + \frac{1}{1 + \lambda \hat{\gamma}^u_1} + (d^u_2 - d^u_1)\hat{\gamma}^u_1, \quad (3.17)
\]

\[
\frac{p^r_1 - c_1 - d^r_2}{p^r_1} = \frac{\lambda}{1 + \lambda \hat{\gamma}^r_1} + \frac{1}{1 + \lambda \hat{\gamma}^r_1} + (d^r_2 - d^r_1)\hat{\gamma}^r_1, \quad (3.18)
\]

with $\hat{\gamma}^u_1 > 0$ and $\hat{\gamma}^r_1 < 0$.

The structure of price under constrained access is similar to the structure under access. The main difference is that the $\hat{\gamma}$ terms are weighted by the difference in the marginal costs of delivery.

We now consider under which conditions the regulator chooses access and bypass on the market.

**Proposition 3.2** When the regulator takes into account the impact of the access price on the entrant’s delivery method, the efficient delivery method is access for $d^u_1 \leq d^u_2$ and bypass for $d^u_1 \geq d^u_2$.

**Proof** (1) For $d^u_1 \leq d^u_2$, by the same argument as in the proof of Proposition 3.1, the regulator could choose to set the access price so that $\alpha^u = d^u_2$ and obtain the level of welfare $W^a \geq W^b$. By a revealed preference argument, the regulator always prefers access to bypass.

(2) For $d^u_1 \geq d^u_2$, we will show that $W^b \geq W^a$ (with strict inequality if $d^u_1 > d^u_2$), so that the regulator prefers bypass to access. Consider the optimal choice of prices under access, and let $p^{u\text{a}}_1 = p^{u\text{a}}_1$, $p^{r\text{a}}_1 = p^{r\text{a}}_1$. Notice that $p^u_2 = d^u_2 + c_2 = c_2 + \alpha^u$ both under bypass and access. Let $\bar{W}^b$ be the
welfare value of bypass under these prices. Because \( d_u^2 \leq d_u^1 \), \( W^a \leq W^b \).

Now, notice that \( \Pi^b_1 = \Pi^a_1 + (d_u^u - d_u^2) x_2 \geq \Pi^a_1 = 0 \), so these prices are feasible in the case of bypass. Again, by a revealed preference argument, we have: \( W^b \geq W^a \geq W^b \).

Notice that, if \( d_u^2 = d_u^1 \), then \( W^a = W^b \). In fact, if \( d_u^2 = d_u^1 \), the optimal choices of \( p_u^u \) and \( p_r^1 \) are the same under access and bypass, because the two problems faced by the regulator are exactly identical. ■

This shows that the regulator will always promote bypass if \( d_u^2 \leq d_u^1 \) and access if \( d_u^2 \geq d_u^1 \). This is the technologically efficient choice, but it is not welfare maximizing. If he could, the regulator would like to favor access for some values such that \( d_u^u \leq d_u^2 \). On the other hand, the regulator will never want to favor bypass for some values such that \( d_u^2 \geq d_u^a \). So there might be excess bypass, but there will never be excess access.

This proposition shows that, if the entrant can freely choose his delivery method, he will base his decision on the comparison between marginal costs of delivery, not taking into account the USO of the incumbent. This will result in excess bypass, and in a lower level of welfare than when the regulator can choose the delivery method of the entrant. This welfare loss will not arise when the delivery cost of the entrant is high (namely when \( d_u^u \geq \alpha^* \)). If \( d_u^a \leq d_u^u < \alpha^* \), the regulator will be forced to lower his access price below the second-best level (from \( \alpha^* \) to \( d_u^2 \)). If \( d^* \leq d_u^u < d_u^a \), the regulator will have to accept bypass whereas she would have preferred access. Finally, for low values of \( d_u^2 \) for which bypass is optimal and feasible, there is no welfare loss, as bypass is always preferred by the regulator. We summarize this discussion with the following figure.

Example 3.2 Example 3.1 continued

We now compare welfare when the regulator can choose the delivery method and faces constrained access. The following graph shows the value
of welfare for the same parameter values as in Example 3.1. We focus on the region of delivery costs of the entrant where the two welfare levels are different.

Figure 2: Constrained access and optimal delivery method

Figure 3: Welfare levels under access, constrained access and bypass.

The solid line denotes welfare with constrained access and the dashed line welfare when the regulator chooses the delivery method. It appears that most of the welfare loss occurs when the two delivery costs are very close.
For $0.498 \leq d_2^u \leq 0.5$, the welfare loss is due to the fact that the regulator faces bypass and prefers access; for $0.5 \leq d_2^u \leq 0.515$, the welfare loss is due to the fact that the regulator must charge an access price $\alpha = d_2^u$ which is below the optimal access charge.

In this section, we have shown that the socially efficient delivery method does not coincide with the technologically efficient one. If the regulator selects the optimal (or Ramsey) prices, ignoring the impact of prices on the delivery choice, there is too much bypass from both a social and technological point of view. Once, the regulator takes into account the impact of the access price on the access vs. bypass decision of the entrant, it implements a technologically efficient delivery method for the entrant but, still, there is too much bypass from a social point of view.

4 Extensions

4.1 Uniform tariff

In the postal sector, a geographically uniform tariff is often imposed as part of the universal service obligations. When a unique stamp price $p_1$ is applied for urban and rural mails, urban mails are relatively more expensive while rural mails are relatively less expensive: $p_1^u \leq p_1 \leq p_1^r$. What are the consequence of the uniform tariff on the access vs bypass decision of the entrant?

A higher urban price means that with a given price $p_2^u$, the entrant is able to capture a larger fraction of the incumbent’s customers. As a consequence, the USP has lower receipts from its urban mail. To compensate, the entrant should contribute more to the USO financing. That is the access price must increase. If we take the first order condition of the maximization of $W^a$, when a uniform tariff is imposed (3.6) must be replaced by:

$$\alpha^u = d_1^u + \frac{\lambda}{1 + \lambda \eta_2^u} + \underbrace{(p_1 - c_1 - d_1^u)\sigma^u}_{\text{higher displacement term}}$$

(4.19)
In this expression, it is clear that the displacement term is higher when a uniform tariff is imposed. And therefore, the optimal access price \( \alpha^* \) increases when the firm cannot price discriminate between its rural and its urban mail.

But, since firm 2 chooses to bypass whenever \( d_2^u \leq \alpha^* \), an increase in the access price implies that the set of parameter under which the entrant has incentives to bypass is larger. In other words, it means that if the regulator wants to implement an efficient technological choice by the entrant, the constrained access solution applies for a larger set of parameters under a uniform tariff. This is represented in the figure 4.

![Figure 4: Efficient access vs bypass choice in the uniform and the non-uniform tariff case](image)

By using the same argument as in proposition 3.2, we can show that the efficient delivery method is the technologically efficient one: bypass for \( d_2^u < d_1^u \) and access otherwise.

The uniform tariff is by itself a source of decrease in the welfare. But, when the entry mode is taken as endogenous, to have an efficient technological choice, the constrained access should be applied for a larger set of parameters. Then, there is an additional welfare loss associated with a geographically uniform tariff: whenever the entrant’s delivery cost lies in \([d_1^u, \alpha^*]\), the welfare is \( \bar{W}^a \) which is lower than the welfare with unconstrained access \( W^a \).
4.2 Uncertainty

We now investigate the consequences of technological uncertainty on the optimal prices and the induced choice of delivery by the entrant. This part of the paper is motivated by the facts that (1) competition in the delivery activity is still at its infancy and (2) the business model of the entrant is different from the incumbent’s one. Therefore, the regulator might have incomplete information on the entrant’s precise delivery cost and we show in this section that this lack of information could be a source of inefficient bypass by the entrant.

More precisely, we consider the following problem: firm 2, the entrant, is characterized by a delivery cost \( d^u_2 \), which is private information to the firm. However, the distribution of this cost is common knowledge. In particular, we assume that it is commonly known that \( d^u_2 \) is distributed according to a continuous density function \( g(.) \) over the interval \( [d^u_2, \overline{d}_2] \) and \( g(d^u_2) > 0 \) for all \( d^u_2 \) in the considered interval.

The regulator sets the incumbent’s prices ignoring the true value of \( d^u_2 \). Firm 2 observes these prices and decides whether it enters the market with its own delivery network or with access. Then, it sets its price at the corresponding competitive level. We concentrate on the cases where the incumbent’s prices cannot be contingent on the realized value of \( d^u_2 \).\(^{12}\)

The uncertainty on the technology of the entrant translates into an uncertainty on the choice of the delivery method. The key issue in this problem is that the access price \( \alpha^u \) determines the probabilities of access and bypass. In particular, for any \( \alpha^u \in [d^u_2, \overline{d}_2] \), there is a probability \( G(\alpha^u) \) that firm 2 builds up its own delivery network and a probability \( 1 - G(\alpha^u) \) that it uses

\(^{12}\)We do not treat the problem as a mechanism design problem where the regulator offers a menu of prices contingent on the revealed value of the delivery cost. If this mechanism is incentive compatible, the firm truthfully reveals its cost. Instead, we assume that the regulator is bound to use flat stamp and access prices. This could be viewed as an application of the non-discrimination principle imposed by the European directives regarding the organization of the postal sector.
the incumbent’s network, where $G(.)$ is the distribution function associated with $g(.)$: $G(x) = \int_{d_{2\mu}}^{x} g(d_{2\mu})dd_{2\mu}$.

The regulatory problem with unknown cost is then:

$$\max_{p_{1\mu}, p_{1\mu}, \alpha_{\mu}} \hat{W} = \int_{d_{2\mu}}^{\alpha_{\mu}} W^{b_1}(d_{2\mu})dd_{2\mu} + \int_{\alpha_{\mu}}^{d_{2\mu}} W^{a_1}(d_{2\mu})dd_{2\mu}$$

subject to the zero profit constraint for firm 1:

$$\Pi_1 = \int_{d_{2\mu}}^{\alpha_{\mu}} \Pi^{b_1}_1(d_{2\mu})dd_{2\mu} + \int_{\alpha_{\mu}}^{d_{2\mu}} \Pi^{a_1}_1(d_{2\mu})dd_{2\mu} \geq 0$$

$\hat{W}$ is the expected welfare when the entrant’s cost is unknown. It is composed of two terms: the first term is the expected welfare under bypass (the entrant’s cost is in $[d_{2\mu}, \alpha_{\mu}]$); the second term is the welfare under access (the entrant’s cost is in $[\alpha_{\mu}, d_{2\mu}]$). Similarly, the profit of firm 1 is the sum of the expected profit under access and the expected profit under bypass.

We will consider the case in which $d_{1\mu} \leq d_{2\mu} < \alpha^{*}$. That is the case in which under full information the regulator always prefers access. Moreover, to induce this choice under symmetric information, the regulator must apply the constrained access solution for $d_{2\mu} \leq \alpha^{*}$.

We now derive a sufficient condition that guarantees that $\alpha_{\mu} = d_{2\mu}$, that is always access, is not a solution to the above problem. For that, let us denote by $p_{1\mu}$ and $p_{1r}$, the price that a regulator would apply if it wants to induce access when it faces an entrant with a known delivery cost of $d_{2\mu}$. Since $d_{2\mu} < \alpha^{*}$, these prices are given by equations (3.17) and (3.18). We check when $(p_{1\mu}, p_{1r}, \alpha_{\mu} = d_{2\mu})$ is not a solution to our problem.

In this problem, the regulator faces a trade-off between promoting the efficient delivery technology which requires a low access price and raising funds from the entrant to finance the cost of the USO which requires instead a high access charge. We show that there are circumstances in which, the regulator induces 'too much' bypass to increase the financial contribution
of firm 2 in the case of access. Allowing for inefficient bypass is a way to increase the expected financial contribution of the entrant to the USO. Under asymmetric information, the regulator trades-off the contribution of the entrant to the USO financing and the efficient delivery method.

Let us define $\Delta$ as the value of $\frac{\partial(W_u + \lambda \Pi_a)}{\partial \alpha}$ evaluated at the proposed solution $\langle p_u^1, p_r^1, \alpha^u = d_2^u \rangle$.

We can show that:

**Proposition 4.3** When, under symmetric information, access is both technically and socially efficient for all the possible values of $d_2^u$, that is $d_2^u \geq d_1^u$; there is a positive probability of bypass under asymmetric information ($\alpha^u > d_2^u$) if: (1) $d_2^u < \alpha^* < d_2^u$ and (2) $\Delta \geq x_2^u g(d_2^u)(d_2^u - d_1^u)$.

**Proof** See appendix B

This proposition demonstrates that whenever access is the socially preferred delivery method for all the possible realizations of the cost parameter of the entrant, the regulator may nevertheless select an access price that induce a positive probability of bypass. The reason is that promoting access in all the possible circumstances is costly because the regulator must set the access price at the lowest possible level. Then, the regulator allows some bypass to increase the expected access receipts when the firm chooses access. There is a trade-off between an efficient market structure and the USO financing. Uncertainty about the entrant’s cost is then a source of excess bypass.

Gautier and Mitra (2003) have a similar result in a context where an entrant with unknown cost decides between access and no entry. They show that, allowing for an inefficient market structure ex-post (in their case a low probability of entry) is a way to increase the financial contribution of the entrant to the infrastructure financing.

If we have a closer look at the condition that guarantees a positive prob-
ability of bypass, we can establish that this condition is more likely to be met when the gap between the lowest possible delivery cost of the entrant and the incumbent’s marginal delivery cost \((d_2^u - d_1^u)\) is small. The reason is that the left hand side \((\Delta)\) decreases in \((d_2^u - d_1^u)\) while the right hand side increases in this difference. And, when \(d_2^u = d_1^u\), there is, for sure, a positive probability of bypass.

5 Concluding remarks

Most of the literature on efficient access pricing consider the choice of a delivery method by the entrant as given. In this paper, we have shown that the efficient access prices do not necessarily induce the choice of an efficient delivery method. In particular, efficient access prices induce too much bypass.

Then, the regulator should modify these prices to take into account the impact of his pricing decision on the entrant choice. Reducing the access price, and therefore the welfare under access, allows to decrease this too much bypass effect. However, the regulator does not manage to achieve a socially efficient delivery choice but only a technically efficient one.

These prices that lead to this technically efficient choice are based on the delivery cost of the entrant. When the cost of the entrant is unknown, the regulator trades-off the probability of bypass with the expected access receipts; a low access price reducing both. Then, uncertainty is another source of excess bypass.

To conclude this paper, we would like to discuss the welfare implications of the different modes of competition. Competition on the upstream segments of the market (access) is a good thing as long as the entrant offers a differentiated product and/or competition decreases the upstream cost. The case of competing networks (bypass) is more complicated. Bypass raises the welfare only when the entrant cost advantage is high enough. But, in some circumstances, maintaining the USO is not always possible. Preventing by-
pass with lower access price is not always the solution and it is costly in term of welfare. Uncertainty leads to excess bypass. And, when access is bought by both the competitor and the clients\textsuperscript{13}, reducing the access price has a more important impact on the receipts of the incumbent.

There are options that we did not envisaged in this paper. First, the scope of the USO could be changed. If $F$ decreases, the margin on all the products decreases and it therefore lower the incentives to bypass. Reducing the scope of the USO is likely to reduce welfare, but it must be compared with the welfare loss associated with the pricing methods to deter bypass. Second, in the US, the incumbent’s monopoly position on the last mail delivery is maintained and it is a radical solution to prevent efficient and inefficient bypass. But, it does not gives incentives to the incumbent for adopting a more efficient delivery technology unless it has the option to sub-contract delivery (see Panzar, 2005 for a detailed analysis of competition for delivery). Finally, a compensation fund is sometimes envisaged to finance the cost of the USO. Armstrong (2001) proposes to sell access at marginal cost and apply an output tax $t$ to the competitor, irrespective of its delivery method. This is a way to achieve technical efficiency (but not social efficiency) and to attain the welfare level $W^u$ if $t = \alpha^* - d_1^u$. But, with that output tax, the welfare function under bypass shifts to the left by an amount $t$. Therefore, there is still inefficient bypass for $d_2^u \in [d_1^u - t, d_1^u]$.

\textsuperscript{13}Usually, at the same price.
A Derivation of the optimal prices

Let us define the following $2 \times 2$ matrix $A$ and the column vector $b$:

$$
A = \begin{pmatrix}
-x_1^u \eta_1^u & x_1^r p_1^r \eta_1^{ru} \\
x_1^u p_1^u \eta_1^{ur} & -x_1^r \eta_1^r
\end{pmatrix}, \quad b = \begin{pmatrix}
-x_1^u \\
-x_1^r
\end{pmatrix}
$$

From these matrices, we define the $2 \times 2$ matrix $B_i$ as the matrix $A$ where its $i^{th}$ column is replaced by the vector $b$.

The solutions of the equation system

$$
A \begin{pmatrix} X_1 \\ X_2 \end{pmatrix} = b
$$

are:

$$
X_1 = \frac{\det[B_1]}{\det[A]} = \frac{\lambda}{1 + \lambda} \frac{\eta_1^r + \eta_1^{ru}}{\eta_1^r \eta_1^u - \eta_1^{ur} \eta_1^{ru}} = \frac{\lambda}{1 + \lambda} \frac{1}{\eta_1^u} \quad (A.20)
$$

$$
X_2 = \frac{\det[B_2]}{\det[A]} = \frac{\lambda}{1 + \lambda} \frac{\eta_1^r + \eta_1^{ur}}{\eta_1^r \eta_1^u - \eta_1^{ur} \eta_1^{ru}} = \frac{\lambda}{1 + \lambda} \frac{1}{\eta_1^r} \quad (A.21)
$$

To derive these expressions, we made the hypothesis that $dx_i^u/dp_i^r = dx_i^r/dp_i^u$.

A.1 Access

Under access, the first order conditions of the welfare maximization problem can be expressed as:

$$
A \begin{pmatrix} x_2^u p_2^r \eta_2^{ru} \\ x_2^u \eta_2^{ru} \end{pmatrix} = \begin{pmatrix} L_1^u \\ L_1^r \\ L_2^u \end{pmatrix}
$$

The solution is:

$$
L_1^u = \frac{\lambda}{1 + \lambda} \left( \frac{1}{\eta_1^u} + \gamma_1^u \right) \quad (A.22)
$$
where $\gamma_1^u = x_1^r \eta_1^r x_2^u \eta_2^u \frac{p_2^u}{p_1^u} \frac{1}{\eta_1^1} > 0$.

And:

$$L_1^r = \frac{\lambda}{1 + \lambda} \left( \frac{1}{\eta_1^1} + \gamma_1^r \right)$$ (A.23)

where $\gamma_1^r = x_1^u \eta_1^r x_2^u \eta_2^u \frac{p_2^u}{p_1^u} + x_1^r \eta_1^r \left( \frac{\eta_2^u}{\eta_1^1} - 1 \right)$, $\gamma_1^r < 0$ because $\eta_1^r < 0$ and $\eta_1^r < 1$.

### A.2 Bypass

Under bypass, the first order conditions of the welfare maximization problem can be expressed as:

$$A \begin{pmatrix} L_1^u \\ L_1^r \end{pmatrix} = b$$

We immediatly have: $L_1^u = \frac{\text{det}(B_1)}{\text{det}(A)} = \frac{\lambda}{1 + \lambda} \frac{1}{\eta_1^1}$ and $L_1^r = \frac{\text{det}(B_2)}{\text{det}(A)} = \frac{\lambda}{1 + \lambda} \frac{1}{\eta_1^1}$. Firm 2 sets its price at marginal cost: $p_2^u = c_2 + d_2^u$ and the access price is set at a level that induces bypass: $\alpha^u \geq d_2^u$.

### A.3 Constrained access

Under constrained access, we have $\alpha^u = d_2^u$. The rst order conditions of the welfare maximization problem can be expressed as:

$$A \begin{pmatrix} L_1^u \\ L_1^r \end{pmatrix} = b + \begin{pmatrix} -(d_2^u - d_1^u) \frac{dx_2^u}{dp_1^u} \\ 0 \end{pmatrix}$$
The solution is:

\[
L^u_1 = \frac{\det |B_1|}{\det |A|} + \left( d^u_2 - d^u_1 \right) \frac{x^r_1 \eta^u_1 (dx^u_2 / dp^u_1)}{\det |A|} \tag{A.24}
\]

\[
L^r_1 = \frac{\det |B_2|}{\det |A|} + \left( d^u_2 - d^u_1 \right) \frac{p^u_2 / p^u_1 \eta^u_1 (dx^u_2 / dp^u_1)}{\det |A|} \tag{A.25}
\]

\[
L^u_1 = \frac{\det |B_1|}{\det |A|} + \left( d^u_2 - d^u_1 \right) \frac{\eta^u_1 (dx^u_2 / dp^u_1)}{x^r_1 (\eta^u_1 \eta^u_1 - \eta^u_1 \eta^u_1)} \tag{A.26}
\]

\[
L^r_1 = \frac{\det |B_2|}{\det |A|} + \left( d^u_2 - d^u_1 \right) \frac{\eta^u_1 (dx^u_2 / dp^u_1)}{x^r_1 (\eta^u_1 \eta^u_1 - \eta^u_1 \eta^u_1)} \tag{A.27}
\]

### B Proof of proposition 4.3

Integrating by part, the regulator’s objective function can be expressed as:

\[
\max_{p^u_1, p^u_1, \alpha^u} \hat{W} \equiv W^a + \lambda \Pi^a_1 - (1 + \lambda) G(\alpha) (\alpha^u \alpha - d^u_1) x^u_2 - \Gamma,
\]

where \( \Gamma = \int_{d^u_2 = \alpha^u}^{d^u_2 = \alpha^u} G(d^u_2) \left( \frac{\partial W^a}{\partial d^u_2} + \lambda \frac{\partial \Pi^a_1}{\partial d^u_2} \right) dd^u_2. \)

This objective function is the sum of three terms. The first one is equivalent to the objective function of the regulator under access. It is what the regulator can achieve when it does not allow bypass \( (\alpha^u = d^u_2). \) The other two terms measure the impact of allowing bypass with a positive probability. The second term is the expected loss of access receipts. This has an impact on both the welfare and the profit and it therefore explains why it is multiplied by \( (1 + \lambda). \) The third term \( \Gamma \) captures the impact on the welfare and the profit of having a more efficient entrant i.e. an entrant with a lower delivery cost \( d^u_2. \) The entrant’s delivery cost does not affect the welfare and the

\[\text{By integrating by part, the expected delivery cost of the entrant evaluated at the upper bound of the integral (} d^u_2 = \alpha^u \text{) is } G(\alpha^u) \alpha^u. \text{ In order to isolate in the objective function the expression } W^a, \text{ we express this expected delivery cost as the sum of the expected cost under access } G(\alpha^u) d^u_1 \text{ plus } G(\alpha^u) (\alpha^u - d^u_1). \]
profit. Under access since \( p_2^u = \alpha^u + c_2 \), but it affects them under bypass since \( p_2^u = d_2^u + c_2 \). \( \Gamma \) then measures the impact of a change in \( d_2^u \) and therefore of a change in \( p_2^u \) on the objective function.

The first order conditions of the above problem are:

\[
\frac{\partial \hat{W}}{\partial p_1^u} = \frac{\partial (W^a + \lambda \Pi_1^a)}{\partial p_1^a} - (1 + \lambda)G(\alpha)(\alpha^u - d_1^u) \frac{\partial x_2^u}{\partial p_1^a} - \frac{\partial \Gamma}{\partial p_1^a} \quad (B.28)
\]

\[
\frac{\partial \hat{W}}{\partial p_1^r} = \frac{\partial (W^a + \lambda \Pi_1^a)}{\partial p_1^a} - \frac{\partial \Gamma}{\partial p_1^a} \quad (B.29)
\]

\[
\frac{\partial \hat{W}}{\partial \alpha^u} = \frac{\partial (W^a + \lambda \Pi_1^a)}{\partial \alpha^u} - (1 + \lambda)G(\alpha)(\alpha^u - d_1^u) \frac{\partial x_2^u}{\partial \alpha^u} \nonumber
\]

\[
-x_2^u (G'(\alpha^u) + g(\alpha^u)(\alpha^u - d_1^u)) - \frac{\partial \Gamma}{\partial \alpha^u} \quad (B.30)
\]

with the derivatives of \((W^a + \lambda \Pi_1^a)\) given by eqs (3.4), (3.5) and (3.6).

We now derive a condition under which \( \langle p_1^u, p_1^r, \alpha^u = d_2^u \rangle \) is not a solution to the above problem.

If \( \alpha^u = d_2^u \), we have \( G(\alpha^u) = 0 \) and then, for \( k = u, r: \frac{\partial \Gamma}{\partial p_k^1} = 0 \) and \( \frac{\partial \Gamma}{\partial \alpha} = 0 \). Then, by construction (B.28) and (B.29) are both equal to zero. Then, if evaluated at the proposed solution, (B.30) is positive, the regulator increases the welfare by increasing \( \alpha^u \) and the proposed solution is not valid.

Because \( d_2^u \) is smaller than \( \alpha^* \), we have that evaluated at the proposed solution \( \Delta = \frac{\partial (W^a + \lambda \Pi_1^a)}{\partial \alpha^u} > 0 \). Then, a sufficient condition for having \( \alpha^u \geq d_2^u \) is:

\[
\Delta \geq x_2^u g(d_2^u)(d_2^u - d_1^u) \quad (B.31)
\]

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References


